On the practical h-stability of nonlinear systems of differential equations

Boulbaba Ghanmi

Faculty of Science of Gafsa bghanmi@gmail.com

Mots-clés: mots clefs.

In this paper, we present a new type of stability for nonlinear systems of differential equations called practical h-stability. Necessary and sufficient conditions for practical h-stability are given using the Lyapunov theory. Our original results generalize well-known fundamental results: practical exponential stability, practical asymptotic stability and practical stability for nonlinear time-varying systems. In addition, these results are used to study the practical h-stability of two important classes of nonlinear systems, namely perturbed and cascaded systems. The last part is devoted to the study of the problem called problem of practical h-stabilization for certain classes of nonlinear systems.

Références

- [1] V. M. Alekseev. An estimate for the perturbations of the solutions of ordinary differential equations, (Russian). Vestnik Moskov. Univ. Seu. I. Mat. Meh. 2 (1961). 28-36.
- [2] A. Benabdallah, I. Ellouze, & M.A. Hammami. Practical stability of nonlinear time-varying cascade systems. J. Dyn. Control Syst. 15, 45-62 (2009)
- [3] S. K. Choi and N. J. Koo. Asymptotic equivalence between two linear Volterra difference systems. Comput. Math. Appl. 47 (2004), 461-471.
- [4] S. K. Choi, Y. H. Goo and N. J. Koo. Lipschitz stability and exponential asymptotic stability for the nonlinear functional differential systems. Dyn. Syst. Appl. 6 (1997), 397-410.
- [5] S. K. Choi, N. J. Koo and H. S. Ryu. h-stability of differential systems via t_{∞} -similarity. Bull. Korean Math. Soc. 34 (1997), 371-383.
- [6] S. K. Choi, H. G. Goo, N. Koo. h-stability of dynamic equations on time scales with nonregressivity. Abstr. Appl. Anal. (2008).
- [7] S. K. Choi, H. G. Goo, N. Koo. *Variationally Stable Difference Systems*. Journal of Mathematical Analysis and Applications 256, 587-605 (2001).
- [8] S. K. Choi and N. Koo. Variationally stable impulsive differential systems. Dyn. Syst.30 (2015), no. 4, 435-449.
- [9] S. K. Choi and N. Koo. A converse theorem on h-stability via impulsive variational systems. J. Korean Math. Soc. 53 (2016), No. 5, pp. 1115-1131
- [10] G. Garashchenko, V. Pichkur. Properties of optimal sets of practical stability of differential inclusions. Part I. Part II. Journal of Automation and Information Sciences 2006, 38:111.
- [11] B. Ghanmi, N. Hadj Taieb & M.A. Hammami . Growth conditions for exponential stability of time varying perturbed systems. International Journal of Control, (2013), 86:6, 1086-1097
- [12] Y. H. Goo and D. H. Ry. h-stability for perturbed integro-differential systems. J. Chungcheong Math. Soc. 21 (2008), 511-517.
- [13] H. K. Khalil, Nonlinear Systems, 3rd Edition, Prentice Hall, Upper Saddle River, 2002
- [14] J. Lasalle, S. Lefschetz. Stability by Lyapunov Direct Method and Application. Academic Press, New York (1961)
- [15] V. Lakshmikantham, S. Leela, and A. A. Martynyuk. *Practical Stability of Nonlinear Systems*. Singapore: World Scientific, 1990.

- [16] V. Lakshmikantham, S. Leela, and A. A. Martynyuk. Stability Analysis of Nonlinear Systems. Marcel Dekker: New York, 1989.
- [17] V. Lakshmikantham and S. Leela. Differential and Integral Inequalities. Vol I and II, Academic Press, New York, 1969.
- [18] V. Lakshmikantham and S.G. Deo. Method of Variation of Parameters For Dynamic Systems-Volume 1.Gordon and Breach Science Publishers, New Delhi, 1998.
- [19] B. Liu, DJ. Hill. Uniform stability and ISS of discrete-time impulsive hybrid systems. Nonlinear Analysis. Hybrid Systems May 2010; 4(2):319-333.
- [20] A. A. Martynyuk and Z. Sun. *Practical Stability and Its Applications*. Science Press, Beijing (2003) (in Chinese)
- [21] A. A. Martynyuk. Advances in Stability Theory at the End of the 20th Century (Stability and Control: Theory, Methods and Applications), Vol. 13. Taylor and Francis: London, 2003.
- [22] A. A. Martynuk. On exponential stability with respect to some of the variables. Russian Acad. Sci. Dokl. Math. 48 (1994), 1720.
- [23] M. Pinto. Stability of nonlinear differential systems. Applicable Analysis: An International Journal, (1992), 43:1-2, 1-20
- [24] M. Pinto. Perturbations of asymptotically stable differential systems. Analysis, (1984) vol. 4, no. 1-2, pp. 161-175.
- [25] P. Wang and X. Liu. h-Stability for Differential Systems Relative to Initial Time Difference. Abstract and Applied Analysis, vol. (2013).
- [26] T. Yoshizawa. Stability Theory by Liapunov's Second Method. Math. Sot. Japan, Tokyo, (1966).